

Trigonometric equations and inequalities
(Extra homework)

1.) $6 \cos x = \frac{1}{\sin x}$

2.) $3 \sin 2x = 2 \cos x$

3.) $\sin x = \frac{\cos 2x}{2}$

4.) $3 \sin^2 x - 4 \cos^2 x = \frac{\sin 2x}{2}$

5.) $\sin 2x \cdot (\sin x - 1) = \cos x \cdot (\sin x + 2)$

6.) $8 \sin^2 x + 4 \sin 2x + 5 \cos 2x = 8$

7.) $\frac{1}{\sin x} + \frac{1}{\cos x} = 2\sqrt{2}$

8.) $\cos 2x + \sin 2x = -1$

9.) $\operatorname{tg}^2 x - 5 = \frac{1}{\cos x}$

10.) $\operatorname{tg}^2 x + 17 = \frac{10}{\cos x}$

11.) $0 < -3 \sin x + 4$

12.) $\frac{1}{5} \geq -\frac{1}{2} \cos x$

13.) $3 \cdot \operatorname{tg} x \geq 8$

14.) $|\cos x| < \frac{1}{2}$

15.) $\sin x > \cos x$ (where does the graph of sine go above the graph of cosine?)

16.) $\cos\left(\frac{\pi}{6} + x\right) < \frac{1}{2}$

17.) $\operatorname{ctg} x \leq 2$

18.) $\sin x \geq \frac{\sqrt{3}}{2}$